

# NONSTATIONARY ARCH AND GARCH WITH $t$ -DISTRIBUTED INNOVATIONS

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## ABSTRACT

Consistency and asymptotic normality are established for the maximum likelihood estimators in the nonstationary ARCH and GARCH models with general  $t$ -distributed innovations. The results hold for joint estimation of (G)ARCH effects and the degrees of freedom parameter parametrizing the  $t$ -distribution. With  $T$  denoting sample size,  $\sqrt{T}$ -convergence is shown to hold with closed form expressions for the multivariate covariances.

KEYWORDS: ARCH, GARCH, asymptotic normality, asymptotic theory, consistency,  $t$ -distribution, maximum likelihood, nonstationarity.

JEL CLASSIFICATION: C32.

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